

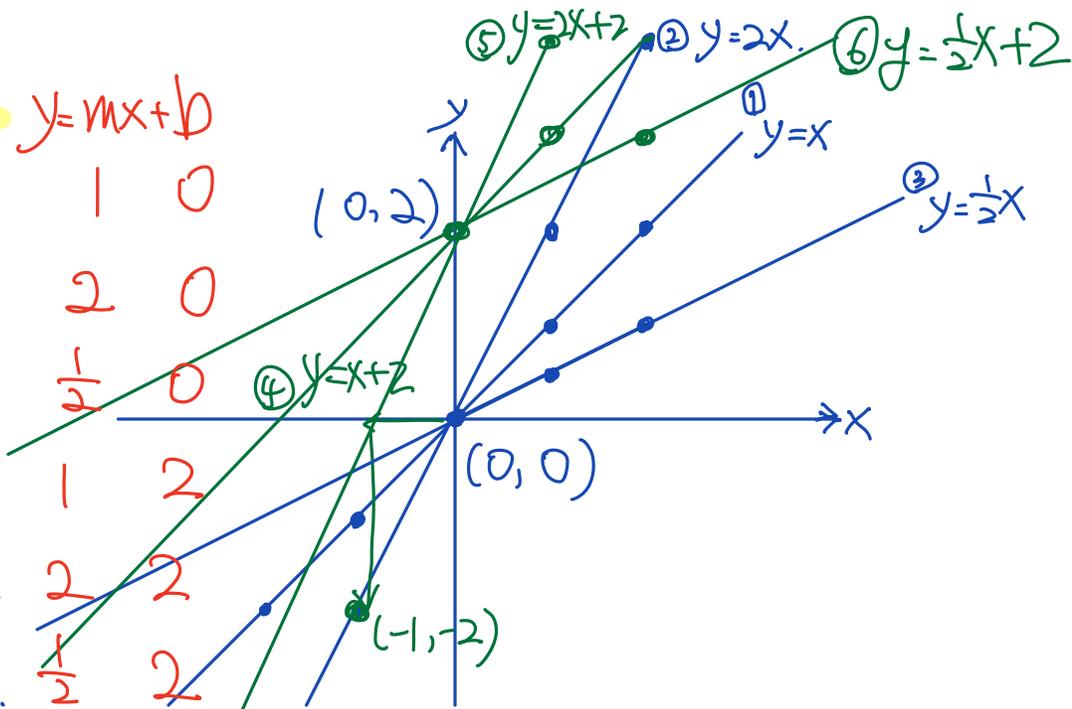
函數的圖形 $y=mx+b$

直線
 $y=mx+b$
 [通式]

- ① $y=1x+0$ 1 0
- ② $y=2x+0$ 2 0
- ③ $y=\frac{1}{2}x+0$ $\frac{1}{2}$ 0
- ④ $y=1x+2$ 1 2
- ⑤ $y=2x+2$ 2 2
- ⑥ $y=\frac{1}{2}x+2$ $\frac{1}{2}$ 2

⑦ $y=|x|$
 ↑
 絕對值

$y=2x$



| | | | | | | | |
|---|---|----|----|---|---|---|---|
| ① | x | -2 | -1 | 0 | 1 | 2 | 3 |
| | y | -2 | -1 | 0 | 1 | 2 | 3 |

| | | | | | | | |
|---|---|----|----|---|---|---|---|
| ② | x | -2 | -1 | 0 | 1 | 2 | 3 |
| | y | -4 | -2 | 0 | 2 | 4 | 6 |

| | | | | |
|---|---|---|---------------|---|
| ③ | x | 0 | 1 | 2 |
| | y | 0 | $\frac{1}{2}$ | 1 |

| | | | | |
|---|---|---|---|---|
| ④ | x | 0 | 1 | 2 |
| | y | 2 | 3 | 4 |

| | | | |
|---|---|---|---|
| ⑤ | x | 0 | 1 |
| | y | 2 | 4 |

| | | | |
|---|---|---|---|
| ⑥ | x | 0 | 2 |
| | y | 2 | 3 |

- ① 代入相同的x
- ② 描點 (x,y) 在坐標平面上
- ③ 連起來

$$y = mx + b$$

1) m 相同的直線平行.

m : 斜率
↓
(有多斜)

2) 直線都通過 $(0, b)$

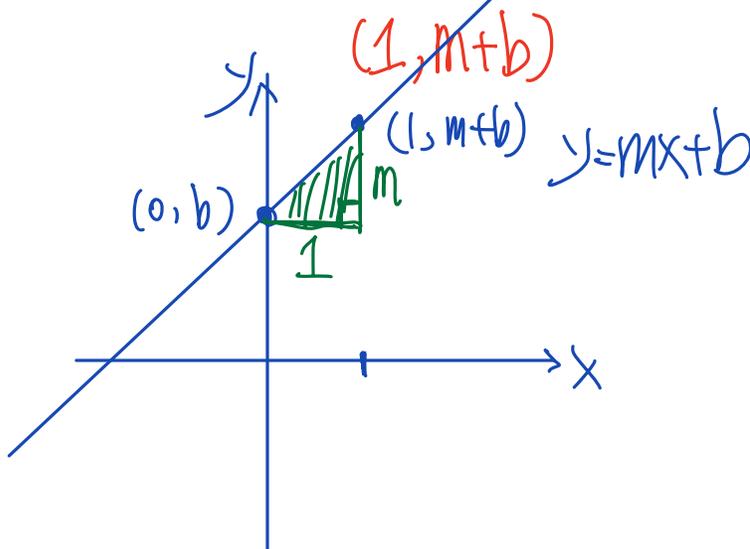
b : y 軸截距

↑
(切)

(切在 y 軸上的 y 座標)

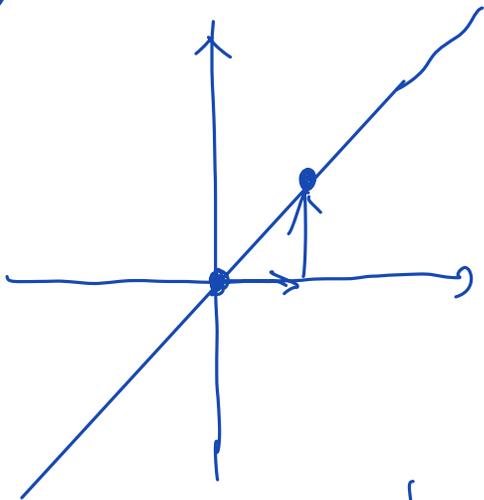
3) 直線一定通過 $(0, b)$

$$\begin{aligned} y &= mx + b \\ &= m + b \end{aligned}$$

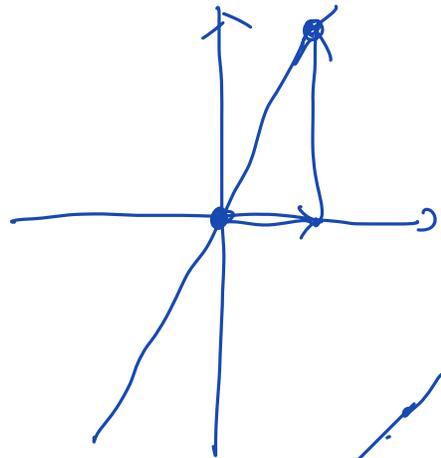


\Rightarrow 又往右走 1 單位時, y 會往上走 m 單位!!

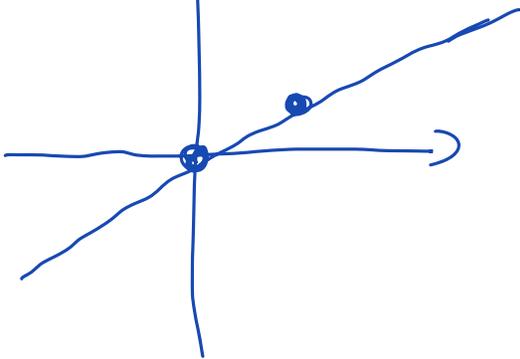
① $y = x + 0$: $\underline{y=0}$ (0,0), $m=1$
 $b=0$



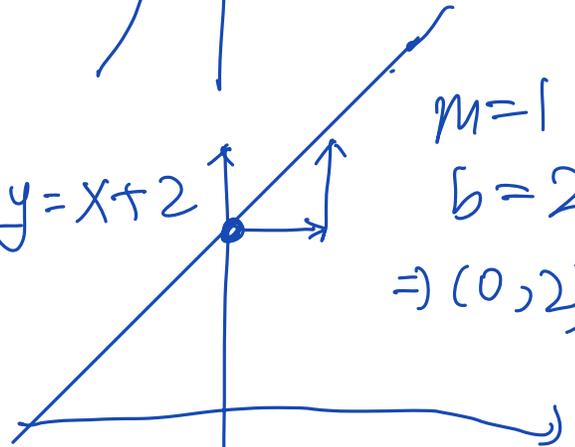
② $y = 2x$, $m=2$
 $b=0$, (0,0)



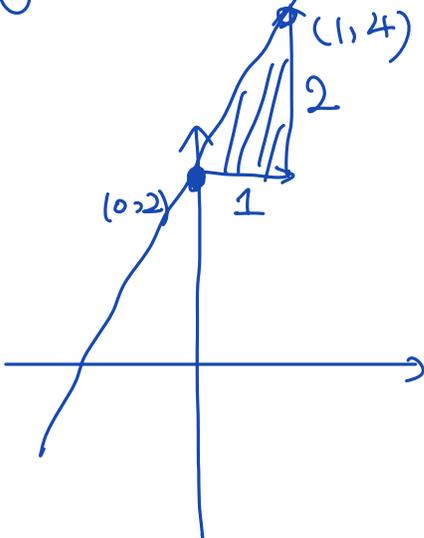
③ $y = \frac{1}{2}x$ $m = \frac{1}{2}$
 $b=0$



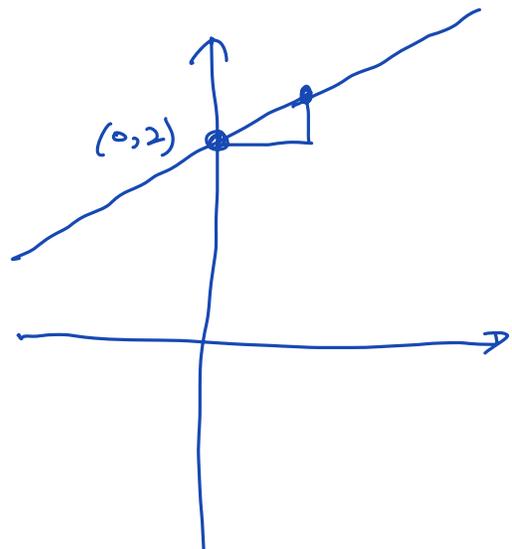
④ $y = x + 2$ $m=1$
 $b=2$
 $\Rightarrow (0,2)$



⑤ $y = 2x + 2$, $m=2$, $b=2 \Rightarrow (0,2)$



⑥ $y = \frac{m}{1}x + \frac{b}{1}$ $m = \frac{1}{2}$ (x slope)
 $b = 2$ (y intercept)



比較係數

$$y = mx + b \text{ (通式)}$$

$$\textcircled{1} \begin{cases} y = 3x + 9 \\ y = mx + b \end{cases}$$

$m=3, b=9$

Step 1. 先寫出通式

Step 2. 一項一項對照 (需做一些處理)

Step 3. 得出通式中的數值

$$\textcircled{2} \begin{cases} y = -2x + 4 \\ y = mx + b \end{cases}$$

$m=-2, b=4$

$$\textcircled{3} \begin{cases} 2x + y = 2 \\ y = mx + b \end{cases} \Rightarrow \begin{cases} y = -2x + 2 \\ y = mx + b \end{cases}$$

$m=-2, b=2$

$$\textcircled{4} \begin{aligned} 3x + 4y &= 5 \\ 4y &= 5 - 3x \\ y &= (5 - 3x) \div 4 \\ y &= \frac{5}{4} - \frac{3}{4}x \end{aligned}$$

$$y = -\frac{3}{4}x + \frac{5}{4}$$
$$y = mx + b$$

$m = -\frac{3}{4}, b = \frac{5}{4}$

↓

$$(0, \frac{5}{4}), (1, \frac{2}{4})$$

$$\textcircled{5} 4x + 3y = 5$$

$$3y = 5 - 4x$$

$$y = \frac{5 - 4x}{3}$$

$$y = \frac{5}{3} - \frac{4}{3}x$$

$$y = -\frac{4}{3}x + \frac{5}{3}$$

$\Rightarrow m = -\frac{4}{3}, b = \frac{5}{3}$

$$\textcircled{6} dx + ey = f$$

$$\Rightarrow ey = f - dx$$

$$\Rightarrow y = \frac{f - dx}{e}$$

$$= \frac{f}{e} - \frac{d}{e}x$$

$$\Rightarrow y = -\frac{d}{e}x + \frac{f}{e}$$

$\Rightarrow m = -\frac{d}{e}, b = \frac{f}{e}$

